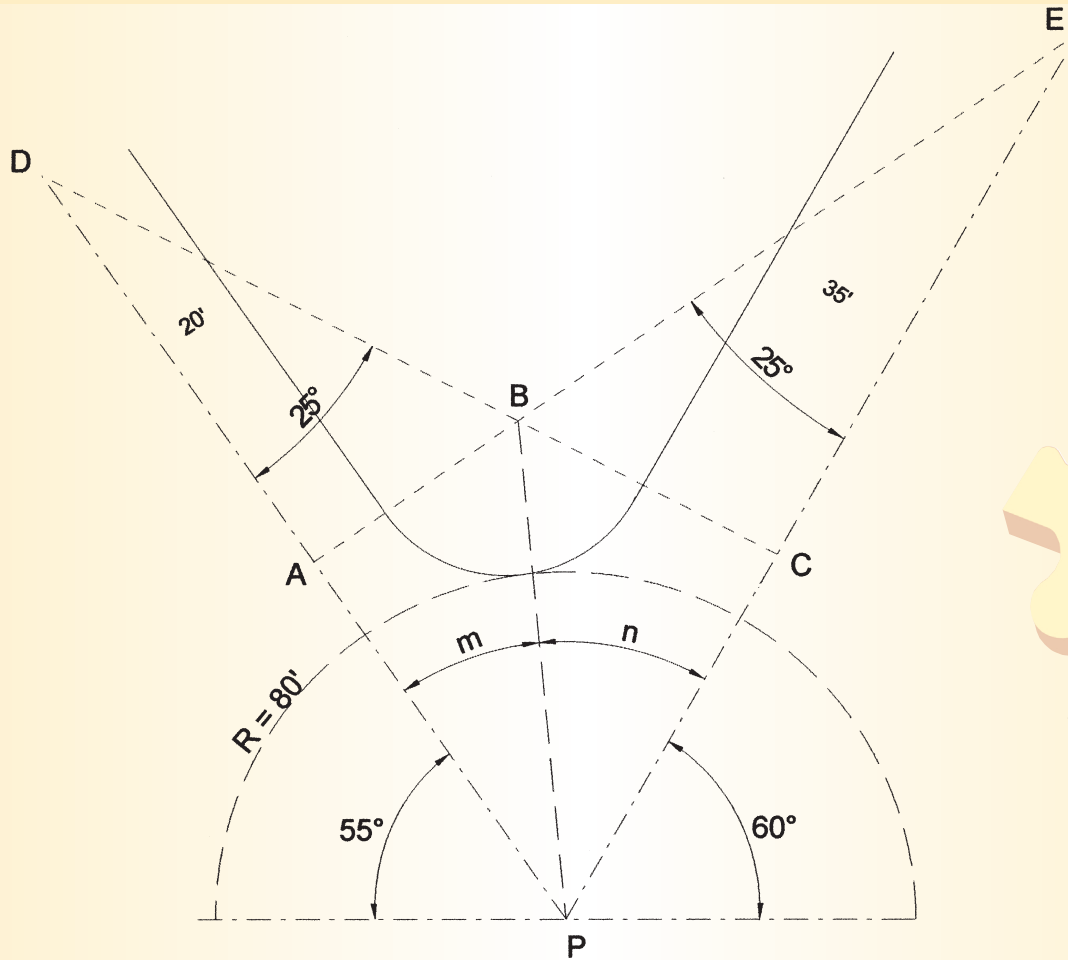


# Solution to Problem 34



$$\sin m = \frac{R + 20}{R + 80}, \quad \sin n = \frac{R + 35}{R + 80}, \quad m + n = 65^\circ$$

$$\sin(m+n) = \sin m \cos n + \sin n \cos m = \sin 65^\circ$$

$$\cos m = \frac{AP}{R + 80}, \quad \cos n = \frac{CP}{R + 80}$$

$$\frac{(R+20)}{(R+80)} \frac{CP}{(R+80)} + \frac{(R+35)}{(R+80)} \frac{AP}{(R+80)} = \sin 65^\circ \quad (\text{Equation \#3})$$

$$\frac{AP}{\sin 25^\circ} = \frac{AE}{\sin 65^\circ} = \frac{(R+20) + (R+35)/\cos 65^\circ}{\sin 65^\circ}$$

$$AP = \frac{\sin 25^\circ (R+20) + (R+35)}{\sin 65^\circ}$$

$$\frac{PC}{\sin 25^\circ} = \frac{CD}{\sin 65^\circ} = \frac{(R+35) + (R+20)/\cos 65^\circ}{\sin 65^\circ}$$

$$PC = \frac{\sin 25^\circ (R+35) + (R+20)}{\sin 65^\circ}$$

which yields, after substituting into Equation #3 and a lot of algebra,

$$2.023842719 R^2 + 25.06500002 R - 3040.254785 = 0$$

from which  $R = 33.0576'$

$$(m = 27^\circ 59' 19.24'' \text{ and } n = 37^\circ 00' 40.76'')$$